

4E : The Quantum Universe

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4E : A Course on the Quantum Universe

- Quantum physics is the most exciting advance in the history of science. Its firestorm like birth and development makes it an excellent example of the symbiosis between theory and experimentation
- It is the fountainhead of Modern Chemistry, Biology and many fields of Engineering
- What to expect in this course:
 - You will see Quantum mechanics a few times as UCSD UG
 - For Example, 130 A,B,C series will be a formal and mathematical account of the methods of quantum Mechanics
 - This course will be a more conceptual and "intuitive" introduction to quantum physics
 - The last part of this course will be a survey of some interesting examples of the Quantum Universe:
 - Particle Physics
 - Astrophysics and Cosmology



4E W	ebsite: http://m	odphys.ucsd.edu/4es05	/
We	UCSD Physic Icome to the Spring '05 Mod	dern Physics (PHYS 4E) Web Site	
	Announcements	Course Handouts	
	Office Hours	Weekly Schedule	
	Homework Solutions	Lecture Slides	
	Quiz & Finals Solutions	[Absolute] Grading Scale	
	Quiz & Final Grades	Scientific American	
	Material on E-Reserve	The Edge of Physics (Free From UCSD location or Proxy)	
	E-Mail: <u>Prof. S</u> Free Stuff You N	harma Jason Wright eed: Acrobat Reader	
Pl. try to a	ccess this website and viewing a	let me know if you have prob any content.	lems

Weekly Schedule

Pl. attend discussion session on Wednesday and problem session on Thursday if you plan to do well in this course

		General Clas	ss Schedul	e
Lecture	Monday	11:00-11:50 am	CNTR 217A	Prof. Sharma
Prof. Office Hour	Monday	1:30 - 2:30 pm	Mayer 3314	Prof. Sharma
Lecture	Tuesday	9:00-9:50 am	SOLIS 109	Prof. Sharma
Prof. Office Hour	Tuesday	2:30-3:30 pm	Mayer 3314	Prof. Sharma
Lecture	Wednesday	11:00-11:50 am	CNTR 217A	Prof. Sharma
Discussion	Wednesday	12:00-12:50 pm	SOLIS 109	Prof. Sharma/Jason Wright
TA Office Hour	Thursday	3:00-4:00 pm	Mayer 2101	Jason Wright
Problem Solving	Thursday	7:00-8:50 pm	SOLIS 111	Jason Wright
Lecture	Friday	11:00-11:50 am	CNTR 217A	Announce Quiz/Midterm Dates
Prof. Office Hour	Weekend	By Appointment	Mayer 3314	Prof. Sharma

Date	Time	Read	Topic	HW problems for the week	Location
Monday	11:00 am	Ch. 3	Quantization of Charge, Light & Energy	Read Section 3.1	CNTR 217A
Tuesday	9:00 am	Ch. 3	Quantization of Charge, Light & Energy	Ch 3: 2,6,11,15,21,22	SOLIS 109
Wednesday	11:00 am	Ch. 3	Quantization of Charge, Light & Energy	Ch 3: 25,32,34,38,41	CNTR 217A
Wednesday	12:00 pm		Discussion		SOLIS 109
Thursday	7:00- 8:50 pm	-	Problem Session	Attempt problems before PS	SOLIS 111
Friday	11:00am	Ch3	Quantization of Charge, Light & Energy	Ch. 3: 42,46	CNTR 217A

Quizzes, Final and Grades

• Course score = 60% Quiz + 40% Final Exam

- 5 quizzes if I can schedule them, best 4 (=n-1) scores used
 - Two problems in each quiz, 45 minutes to do it
 - One problem HW like, other more interesting
 - Closed book exam, but you can bring one page "CHEAT SHEET"
 - Blue Book required, Code numbers will be given at the 1st quiz. Bring calculator, check battery !
 - No makeup quizzes
 - See handout for Quiz regrade protocol
- Final Exam : TBA, but in Week of June 6-10
 - Inform me of possible conflict within 2 weeks of course
 - Don't plan travel/vacation before finals schedule is confirmed !
 - No makeup finals for any reason



Course Grade

- Our wish is that every body gets an A ! ... So no curve
- Grading is on an absolute scale. Roughly it looks like this :

> 85 A+ > 75 A > 60 B > 45 C < 30 F	Total Score	Grade
> 75 A > 60 B > 45 C < 30	> 85	A +
> 60 B > 45 C < 30	> 75	Α
> 45 C < 30 F	> 60	В
< 30 F	> 45	С
	< 30	F

How To Do Well In This Course

- Read the assigned text BEFORE lecture to get a feel of the topic
- Don't rely on your intuition ! The concepts are quite abstract.
- Attend lecture (ask questions during/before/after lecture) and discussion.
- Do not just accept a concept without understanding the logic
- Attempt all homework problems yourself
 - Before looking at the problem solutions (available on web by Tuesday afternoon) & before attending Problem Solving session
- The textbook, the lectures and the discussions are all integral to this course. Just following lectures is not sufficient (I won't cover every thing)
- Quarter goes fast, don't leave every thing for the week before exam !!
- Don't hesitate to show up at Prof. or TA office hour (they don't bite !)

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Constituents of Nature: The Ancient View

Every civilization has speculated about the constitution of the Universe. The Greek philosophers thought that the universe was made up of just four elements: Earth, air, Fire

and Water



This was a great "scientific" theory because it was simple but it had one drawback: It was wrong! There was no experimental proof for it.

Concept of An Atom

- Around 6th-5th century BC, Indians and more famously the Greeks speculated on "indivisible" constituents of matter
- In 5th BC, Leucippus and his follower Democritus set the scene for modern physics by asking "what would happen if you chopped up matter into ever smaller pieces. There would be a limit beyond which you could chop no more!"
- They called this indivisible piece an *Atom (or Anu in Sanskrit)*





Some Highlights in Understanding Matter

- Lavosier's measurement of conservation of matter in chemical reactions
- Faraday's Electrolysis experiment (1833) : Same amount of charge F is required to decompose 1 gram-ionic weight of monovalent ions
 - 1 F passed thru NaCl leads to 23gm of Na at cathode and 35.5gm Cl at anode but it takes 2F to disassociate CuSO₄
 - → Mass of element liberated at an electrode is directly proportional to charge transferred and inversely prop. to the valence of the freed element
- Avagadro postulated that pure gases at same temprature and pressure have same number of molecules per unit volume.

- > N_A=6.023x 10²³

- Dalton & Mendeleev's theory that all elementary atoms differing in mass and chemical properties
- Discovery of cathode rays and measurement of their properties14



















Disaster \rightarrow Experimental observation that could not be explained by Classical theory

- Disaster # 1 : Nature of Blackbody Radiation from your BBQ grill
- Disaster # 2: Photo Electric Effect
- Disaster # 3: Scattering light off electrons (Compton Effect)

Resolution of Experimental Observation will require radical changes in how we think about nature

- → QUANTUM PHYSICS: The Art of Conversation with Subatomic Particles













Classical Calculation

of standing waves between Wavelengths λ and λ +d λ are

N(
$$\lambda$$
)d $\lambda = \frac{8\pi V}{\lambda^4} \bullet d\lambda$; V = Volume of box = L³

Each standing wave contributes energy E = kT to radiation in Box

Energy density $u(\lambda) = [\# \text{ of standing waves/volume}] \times \text{ Energy/Standing Wave}$

$$= \frac{8\pi V}{\lambda^4} \times \frac{1}{V} \times kT = \frac{8\pi}{\lambda^4} kT$$

Radiancy
$$R(\lambda) = \frac{c}{4}u(\lambda) = \frac{c}{4}\frac{8\pi}{\lambda^4} kT = \frac{2\pi c}{\lambda^4} kT$$

Radiancy is Radiation intensity per unit λ interval: Lets plot it

Prediction : as $\lambda \rightarrow 0$ (high frequency f), R(λ) \rightarrow Infinity ! Oops !

















































TABLE 3-1 Photoelectric work functions	
Element	φ (eV)
Na	2.28
С	4.81
Cd	4.07
Al	4.08
Ag	4.73
Pt	6.35
Mg	3.68
Ni	5.01
Se	5.11
Pb	4.14

Reinterpreting Photoelectric Effect With Light as Photons

Photoelectric Effect on An Iron Surface Light of Intensity I = 1.0 μ W/cm² incident on 1.0cm² surface of Fe Assume Fe reflects 96% of light further only 3% of incident light is Violet region (λ = 250nm) barely above threshold frequency for Photoelectric effect (a) Intensity available for Ph. El effect I = 3% × 4% × (1.0 μ W/cm²) (b) how many photo-electrons emitted per second ? # of photoelectrons = $\frac{Power}{h f} = \frac{3\% \times 4\% \times (1.0 \ \mu$ W/cm²) $\lambda}{hc}$ $= \frac{(250 \times 10^{-9} m)(1.2 \times 10^{-9} J/s)}{(6.6 \times 10^{-34} J \cdot s)(3.0 \times 10^8 m/s)}$ 1.5×10^9 (c) Current in Ammeter : i = (1.6 × 10^{-19} C)(1.5 × 10^9) = 2.4 × 10^{-10} A (d) Work Function Φ = hf₀ = (4.14 × 10^{-15} eV \cdot s)(1.1 × 10^{15} s^{-1}) = 4.5 eV

Facts about Light Quantum

- The human eye is a sensitive photon detector at visible wavelengths: Need >5 photons of ≅ 550nm to register on your optical sensor
- The Photographic process :
 Energy to Dissociate an AgBr molecule = 0.6eV
- Photosynthesis Process : 9 sunlight photon per reaction cycle of converting CO₂ and water to carbohydrate & O₂
 chlorophyll absorbs best at λ ≅ 650-700 nm
- Designing Space Shuttle "skin" : Why Platinum is a good thing
- designing Solar cells : picking your metal cathode







$E&M \rightarrow$ that any charged particle will emit radiation when accelerated.

This EM radiation "appears" as photons. Since photo carries energy and momentum, the electron must lose same amount. If all of electron's energy is lost in just one single collision then:






























Constructive Interference depends on Path (or phase) diff. Traversed Two Identical waves $y_i(x,t) = y_{max} \sin(k_i x - \omega_i t + \phi_i)$ travel along +x and interefere to give a resulting wave y'(x,t). The resulting wave form depends on relative phase difference between 2 waves. Shown for $\Delta \phi = 0$, π , π $y_1(x,t)$ $y_1(x, t) = y_2(x, t)$ $= y_1(x, \ell)$ $-y_2(x, t)$ and $y_2(x, t)$ $\phi = 0$ $\phi = \frac{2}{3}\pi$ rad $\phi=\pi \ {\rm rad}$ (b) (a)(c)L y'(x, t)y'(x, l)y'(x, t)

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Allowed Energy Levels & Orbit Radii in Bohr Model	
$E=KE+U = \frac{1}{2}m_e v^2 - k\frac{e^2}{r}$	Radius of Electron Orbit :
Force Equality for Stable Orbit	$mvr = n\hbar$
\Rightarrow Coulomb attraction = CP Force	$\Rightarrow v = \frac{n\hbar}{mr},$
$k \frac{e^2}{r^2} = \frac{m_e v^2}{r}$ $\Rightarrow KE = \frac{m_e v^2}{2} = k \frac{e^2}{2r}$	substitute in KE= $\frac{1}{2}m_e v^2 = \frac{ke^2}{2r}$ $\Rightarrow r_n = \frac{n^2\hbar^2}{mke^2}, n = 1, 2,\infty$
Total Energy $E = KE + U = -k \frac{e^2}{2r}$	$n = 1 \Rightarrow \text{Bohr Radius } a_0$
Negative $E \Rightarrow$ Bound system	$a_0 = \frac{1^2 \hbar^2}{mke^2} = 0.529 \times 10^{-10} m$
This much energy must be added to	In general $r_n = n^2 a_0; n = 1, 2,, \infty$
the system to break up the bound atom	Quantized orbits of rotation
Total Energy $E = KE+U= -k \frac{e^2}{2r}$ Negative $E \Rightarrow$ Bound system This much energy must be added to the system to break up the bound atom	$n = 1 \Longrightarrow \text{Bonr Radius } a_0$ $a_0 = \frac{1^2 \hbar^2}{mke^2} = 0.529 \times 10^{-10} m$ In general $r_n = n^2 a_0; n = 1, 2, .$ Quantized orbits of rotation









Some Notes About Bohr Like Atoms

- Ground state of Hydrogen atom (n=1) E_0 = -13.6 eV
- Method for calculating energy levels etc applies to all Hydrogenlike atoms → -1e around +Ze
 - Examples : He⁺, Li⁺⁺
- Energy levels would be different if replace electron with Muons
 - Reduced Mass
 - Necessity of Reduced Mass calculation enhanced for "positronium" like systems
- Bohr's method can be applied in general to all systems under a central force (e.g. gravitational instead of Coulombic)

If change
$$U(r) = k \frac{Q_1 Q_2}{r} \rightarrow G \frac{M_1 M_2}{r}$$

Changes every thing: E, r, f etc
"Importance of constants in your life"

<text><list-item><list-item><list-item><list-item>









Prince Louise de Broglie & Matter Waves

- · Key to Bohr atom was Angular momentum quantization
- Why this Quantization: $mvr = |L| = nh/2\pi$?
- Invoking symmetry in nature, Prince Louise de Broglie conjectured:

Because photons have wave <u>and</u> particle like nature \rightarrow particles may have <u>wave</u> like properties !!

Electrons have accompanying "pilot" wave (not EM) which guide particles thru spacetime.



A PhD Thesis Fit For a Prince !

- Matter Wave !
 - -"Pilot wave" of $\lambda = h/p = h / (\gamma m v)$
 - Frequency of pilot wave f = E/h

• Consequence:

- If matter has wave like properties then there would be interference (destructive & constructive) of some kind!
 - Analogy of standing waves on a plucked string to explain the quantization condition of Bohr orbits





















































Measurement Error : $x \pm \Delta x$

- Measurement errors are unavoidable since the measurement procedure is an experimental one
- True value of an measurable quantity is an abstract concept
- In a set of repeated measurements with random errors, the distribution of measurements

resembles a Gaussian distribution characterized by the parameter σ or Δ characterizing the width of the distribution f(x)
























Resolving Power of Light Thru a Lens

Image of 2 separate point sources formed by a converging lens of diameter d, ability to resolve them depends on λ & d because of the Inherent diffraction in image formation



















































Summary of Experiments So Far

- 1. Probability of an event is given by the square of amplitude of a complex $\# \Psi$: Probability Amplitude
- 2. When an event occurs in several alternate ways, probability amplitude for the event is sum of probability amplitudes for each way considered seperately. There is interference:

$$\Box \quad \Psi = \Psi_1 + \Psi_2$$

 $P_{12} = |\Psi_1 + \Psi_2|^2$

- 3. If an experiment is done which is capable of determining whether one or other alternative is actually taken, probability for event is just sum of each alternative
 - Interference pattern is LOST !





Losing Out To Uncertainty Principle

- To measure the RECOIL of the wall \Rightarrow
 - must know the initial momentum of the wall before electron hit it
 - Final momentum after electron hits the wall
 - Calculate vector sum \rightarrow recoil
- Uncertainty principle :
 - To do this $\Rightarrow \Delta P = 0 \rightarrow \Delta X = \infty$ [can not know the position of wall exactly]
 - If don't know the wall location, then down know where the holes are
 - Holes will be in different place for every electron that goes thru
 - → The center of interference pattern will have different (random) location for each electron
 - Such random shift is just enough to Smear out the pattern so that no interference is observed !

Summary

- Probability of an event in an ideal experiment is given by the square of the absolute value of a complex number Ψ which is call probability amplitude
 - P = probability
 - Ψ = probability amplitude, P=| Ψ |²
- When an even can occur in several alternative ways, the probability amplitude for the event is the sum of the probability amplitudes for each way considered separately. There is interference:

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-\Psi = \Psi_1 + \Psi_2
```

 $P = |\Psi_1 + \Psi_2|^2$

• If an experiment is performed which is capable of determining whether one or other alternative is actually taken, the probability of the event is the sum of probabilities for each alternative. The interference is lost: $P = P_1 + P_2$







 $-P = |\Psi^* \Psi| = |\Psi_1|^2 + |\Psi_2|^2 + 2|\Psi_1|\Psi_2| \cos\phi$

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- Act of Observation destroys the system (No watching!)
- If can't watch then all conversations can only be in terms of Probability P
- Every particle under the influence of a force is described by a Complex wave function Ψ(x,y,z,t)
- Ψ is the ultimate DNA of particle: contains all info about the particle under the force (in a potential e.g Hydrogen)
- Probability of per unit volume of finding the particle at some point (x,y,z) and time t is given by

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- P(x,y,z,t) = \Psi(x,y,z,t) \cdot \Psi^*(x,y,z,t) = |\Psi(x,y,z,t)|^2
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• When there are more than one path to reach a final location then the probability of the event is

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-\Psi = \Psi_1 + \Psi_2
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- P = |\Psi^* \Psi| = |\Psi_1|^2 + |\Psi_2|^2 + 2 |\Psi_1| |\Psi_2| \cos\phi
```

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Normalization Condition: Particle Must be Somewhere

Example: $\psi(x,0) = Ce^{-\left|\frac{x}{x_0}\right|}$, C & x_0 are constants This is a symmetric wavefunction with diminishing amplitude The Amplitude is maximum at $x = 0 \Rightarrow$ Probability is max too Normalization Condition: How to figure out C ?

A real particle must be somewhere: Probability of finding particle is finite

$$P(-\infty \le x \le +\infty) = \int_{-\infty}^{+\infty} |\psi(x,0)|^2 dx = \int_{-\infty}^{+\infty} C^2 e^{-2\left|\frac{x}{x_0}\right|} dx = 1$$

$$\Rightarrow 1 = 2C^2 \int_{0}^{\infty} e^{-2\left|\frac{x}{x_0}\right|} dx = 2C^2 \left[\frac{x_0}{2}\right] = C^2 x_0$$

$$\Rightarrow \overline{\psi'(x,0)} = \frac{1}{\sqrt{x_0}} e^{-\frac{|x|}{x_0|}}$$

























































Table 5.2Common Observables and Associated Operators		
Observable	Symbol	Associated Operator
position	X	x
momentum	Þ	$\frac{\hbar}{i}\frac{\partial}{\partial x}$
potential energy	U	U(x)
kinetic energy	K	$-rac{\hbar^2}{2m}rac{\partial^2}{\partial x^2}$
hamiltonian	Н	$-\frac{\hbar^2}{2m}\frac{\partial^2}{\partial x^2}+U(x)$
total energy	E	$i\hbar \frac{\partial}{\partial t}$

Use State Solution

$$\begin{aligned}
\text{P} &= \hat{h} \quad \frac{d}{dx} & \text{Momentum Operator} \\
\text{gives the value of average mometum in the following way:} \\
& = \int_{-\infty}^{+\infty} \psi^*(x)[p]\psi(x)dx = \int_{-\infty}^{+\infty} \psi^*(x) \left(\frac{h}{i}\right) \frac{d\psi}{dx} dx \\
\text{Similerly :} \\
&[K] \text{ or } \hat{K} = -\frac{\hbar^2}{2m} \frac{d^2}{dx^2} \text{ gives the value of average KE} \\
&< K> = \int_{-\infty}^{+\infty} \psi^*(x)[K]\psi(x)dx = \int_{-\infty}^{+\infty} \psi^*(x) \left(-\frac{\hbar^2}{2m} \frac{d^2\psi(x)}{dx^2}\right) dx \\
\text{Similerly} \\
 = \int_{-\infty}^{+\infty} \psi^*(x)[U(x)]\psi(x)dx : \text{ plug in the U(x) fn for that case} \\
&\text{ and } = \int_{-\infty}^{+\infty} \psi^*(x)[K+U(x)]\psi(x)dx = \int_{-\infty}^{+\infty} \psi^*(x) \left(-\frac{\hbar^2}{2m} \frac{d^2\psi(x)}{dx^2} + U(x)\right) dx \\
&\text{ Hamiltonian Operator } [H] = [K] + [U] \\
&\text{ The Energy Operator } [E] = i\hbar \frac{\partial}{\partial t} \text{ informs you of the average energy} \end{aligned}$$
[H] & [E] Operators

- [H] is a function of x
- [E] is a function of tthey are really different operators
- But they produce identical results when applied to any solution of the time-dependent Schrodinger Eq.
- $[H]\Psi(x,t) = [E] \Psi(x,t)$

$$\left[-\frac{\hbar^2}{2m}\frac{\partial^2}{\partial x^2} + U(x,t)\right]\Psi(x,t) = \left[i\hbar\frac{\partial}{\partial t}\right]\Psi(x,t)$$

• Think of S. Eq as an expression for Energy conservation for a Quantum system

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Where do Operators come from ? A touchy-feely answer
Example: [p] The momentum Extractor (operator):
Consider as an example: Free Particle Wavefunction

$$\Psi(x,t) = Ae^{i(kx-wt)}$$
; $k = \frac{2\pi}{\lambda}$, $\lambda = \frac{h}{p} \Rightarrow k = \frac{p}{h}$
rewrite $\Psi(x,t) = Ae^{i(\frac{p}{h}x-wt)}$; $\frac{\partial\Psi(x,t)}{\partial x} = i\frac{p}{h}Ae^{i(\frac{p}{h}x-wt)} = i\frac{p}{h}\Psi(x,t)$
 $\Rightarrow \left[\frac{\hbar}{i}\frac{\partial}{\partial x}\right]\Psi(x,t) = p\Psi(x,t)$
So it is not unreasonable to associate $[p] = \left[\frac{\hbar}{i}\frac{\partial}{\partial x}\right]$ with observable p



But what about the $\langle KE \rangle$ of the Particle in Box ? $\langle p \rangle = 0$ so what about expectation value of $K = \frac{p^2}{2m}$? $\langle K \rangle = 0$ because $\langle p \rangle = 0$; clearly not, since we showed $E = KE \neq 0$ Why? What gives ? Because $p_n = \pm \sqrt{2mE_n} = \pm \frac{n\pi\hbar}{L}$; "±" is the key! The AVERAGE p = 0, since particle is moving back & forth $\langle KE \rangle = \langle \frac{p^2}{2m} \rangle \neq 0$; not $\frac{\langle p^2 \rangle}{2m}$! Be careful when being "lazy" Quiz: what about $\langle KE \rangle$ of a quantum Oscillator? Does similar logic apply??



 $P(x,t) = \Psi^* \Psi = \psi^*(x) \ e^{\frac{iE}{\hbar}t} \psi(x) \ e^{\frac{iE}{\hbar}t} = \psi^*(x)\psi(x)e^{\frac{iE}{\hbar}t - \frac{iE}{\hbar}t} = |\psi(x)|^2$ In such cases, P(x,t) is INDEPENDENT of time. These are called "stationary" states because Prob is independent of time Examples : Particle in a box (why?) : Quantum Oscillator (why?) Total energy of the system depends on the spatial orientation of the system : charteristic of the potential situation !





Quantum Picture: Harmonic Oscillator
Find the Ground state Wave Function $\psi(x)$
Find the Ground state Energy E when $U(x) = \frac{1}{2}m\omega^2 x^2$
Time Dependent Schrödinger Eqn: $\frac{-\hbar^2}{2m}\frac{\partial^2\psi(x)}{\partial^2 x} + \frac{1}{2}m\omega^2 x^2\psi(x) = E \ \psi(x)$
$\Rightarrow \frac{d^2 \psi(x)}{dx^2} = \frac{2m}{\hbar^2} (E - \frac{1}{2}m\omega^2 x^2) \psi(x) = 0$ What $\psi(x)$ solves this?
Two guesses about the simplest Wavefunction:
1. $\psi(x)$ should be symmetric about x 2. $\psi(x) \to 0$ as $x \to \infty$
+ $\psi(x)$ should be continuous & $\frac{d\psi(x)}{dx}$ = continuous
My guess: $\psi(\mathbf{x}) = C_0 e^{-\alpha x^2}$; Need to find $C_0 \& \alpha$:
What does this wavefunction & PDF look like?



Time Independent Sch. Eqn & The Harmonic Oscillator
Master Equation is :
$$\frac{\partial^2 \psi(x)}{\partial x^2} = \frac{2m}{\hbar^2} [\frac{1}{2}m\omega^2 x^2 - E]\psi(x)$$

Since $\psi(x) = C_0 e^{-\alpha x^2}$, $\frac{d\psi(x)}{dx} = C_0 (-2\alpha x)e^{-\alpha x^2}$,
 $\frac{d^2 \psi(x)}{dx^2} = C_0 \frac{d(-2\alpha x)}{dx} e^{-\alpha x^2} + C_0 (-2\alpha x)^2 e^{-\alpha x^2} = C_0 [4\alpha^2 x^2 - 2\alpha]e^{-\alpha x^2}$
 $\Rightarrow C_0 [\frac{4\alpha^2 x^2}{dx^2}] - [2\alpha] e^{-\alpha x^2} = \frac{2m}{\hbar^2} [\frac{1}{2}m\omega^2 x^2] - E]C_0 e^{-\alpha x^2}$
Match the coeff of x^2 and the Constant terms on LHS & RHS
 $\Rightarrow 4\alpha^2 = \frac{2m}{\hbar^2} \frac{1}{2}m\omega^2$ or $\alpha = \frac{m\omega}{2\hbar}$
& the other match gives $2\alpha = \frac{2m}{\hbar^2} E$, substituing $\alpha \Rightarrow$
 $E = \frac{1}{2}\hbar\omega = hf$!!!!.....(Planck's Oscillators)
What about C_0 ? We learn about that from the Normalization cond.









































$$\begin{aligned} &Radioactivity Explained Crudely\\ T(E) &\approx e^{\left[\frac{-2}{h}\sqrt{2m}\int\sqrt{U(x)-E}\ dx\right]}, U(x) = \frac{2e^2Z}{4\pi\varepsilon_0 r}\\ &\ln T = \frac{-2}{\hbar} \int_0^b \sqrt{2m_\alpha} \left(\frac{2e^2Z}{4\pi\varepsilon_0 r} - E_\alpha\right) dr,\\ &\text{limits of integration correspond to values of r when } E=U\\ &\Rightarrow \frac{2e^2Z}{4\pi\varepsilon_0 b} = E \Rightarrow \left[b = \frac{2e^2Z}{4\pi\varepsilon_0 E_\alpha}\right]\\ &\text{Define } \xi = \frac{r}{b}; = \frac{r}{2e^2Z/4\pi\varepsilon_0 E} \Rightarrow \ln T \cong \frac{-2\left(\sqrt{2m_\alpha E}\right)b}{\hbar} \int_0^1 \sqrt{\frac{1}{\xi}-1} \ d\xi\\ &\text{Substitute } \xi = \sin^2\theta \text{ in integration, change limits } \Rightarrow\\ &\ln T \cong \frac{-4\left(\sqrt{2m_\alpha E_\alpha}\right)b}{\hbar} \left[\int_0^{\pi/2} \cos^2\theta d\theta\right]; use \int_0^{\pi/2} \cos^2\theta d\theta = \pi/4 \& E_\alpha = \frac{m_\alpha V_\alpha^2}{2}\\ &\ln T \cong \frac{-2\pi}{\hbar} \frac{Ze^2}{4\pi\varepsilon_0} \sqrt{\frac{2m_\alpha}{E_\alpha}} = \frac{-4\pi}{\hbar} \frac{Ze^2}{4\pi\varepsilon_0} \frac{1}{V_\alpha} \Rightarrow \frac{T \cong e^{\left[\frac{-4\pi}{\hbar} \ 4\pi\varepsilon_0 V_\alpha\right]}}{T \cong e^{\left[\frac{-4\pi}{\hbar} \ 4\pi\varepsilon_0 V_\alpha\right]}}\\ &\Rightarrow \frac{T \propto e^{\frac{-1}{V_\alpha}} \ and \ T \propto e^{-z}}{\pi} \quad ...SHARP \ DEPENDENCE!! \end{aligned}$$

























Particle in 3D Rigid Box : Separation of Orthogonal Spatial (x,y,z) Variables
TISE in 3D: $-\frac{\hbar^2}{2m}\nabla^2\psi(x, y, z) + U(x, y, z)\psi(x, y, z) = E\psi(x, y, z)$
x,y,z independent of each other, write $\psi(x, y, z) = \psi_1(x)\psi_2(y)\psi_3(z)$
and substitute in the master TISE, after dividing thruout by $\psi = \psi_1(x)\psi_2(y)\psi_3(z)$
and noting that U(r)=0 for $(0 \le x, y, z, \le L) \Rightarrow$
$\left(-\frac{\hbar^2}{2m}\frac{1}{\psi_1(x)}\frac{\partial^2\psi_1(x)}{\partial x^2}\right) + \left(-\frac{\hbar^2}{2m}\frac{1}{\psi_2(y)}\frac{\partial^2\psi_2(y)}{\partial y^2}\right) + \left(-\frac{\hbar^2}{2m}\frac{1}{\psi_3(z)}\frac{\partial^2\psi_3(z)}{\partial z^2}\right) = E = Const$
This can only be true if each term is constant for all x,y,z \Rightarrow
$\frac{-\frac{\hbar^2}{2m}\frac{\partial^2\psi_1(x)}{\partial x^2} = E_1\psi_1(x)}{\partial x^2}; \frac{-\frac{\hbar^2}{2m}\frac{\partial^2\psi_2(y)}{\partial y^2} = E_2\psi_2(y)}{\partial y^2}; \frac{-\frac{\hbar^2}{2m}\frac{\partial^2\psi_3(z)}{\partial z^2} = E_3\psi_3(z)}{\partial z^2}$
With $E_1 + E_2 + E_3 = E$ =Constant (Total Energy of 3D system)
Each term looks like particle in 1D box (just a different dimension)
So wavefunctions must be like $\psi_1(x) \propto \sin k_1 x$, $\psi_2(y) \propto \sin k_2 y$, $\psi_3(z) \propto \sin k_3 z$



Particle in 3D Box : Wave function Normalization Condition

$$\Psi(\vec{r},t) = \psi(\vec{r}) e^{i\frac{E}{\hbar}t} = A [\sin k_1 x \sin k_2 y \sin k_3 z] e^{i\frac{E}{\hbar}t}$$

$$\Psi^*(\vec{r},t) = \psi^*(\vec{r}) e^{i\frac{E}{\hbar}t} = A [\sin k_1 x \sin k_2 y \sin k_3 z] e^{i\frac{E}{\hbar}t}$$

$$\Psi^*(\vec{r},t) \Psi(\vec{r},t) = A^2 [\sin^2 k_1 x \sin^2 k_2 y \sin^2 k_3 z]$$
Normalization Condition : $1 = \iiint_{xyz} P(r) dx dy dz \Rightarrow$

$$1 = A^2 \int_{x=0}^{L} \sin^2 k_1 x dx \int_{y=0}^{L} \sin^2 k_2 y dy \int_{z=0}^{L} \sin^2 k_3 z dz = A^2 \left(\sqrt{\frac{L}{2}}\right) \left(\sqrt{\frac{L}{2}}\right) \left(\sqrt{\frac{L}{2}}\right)$$

$$\Rightarrow A = \left[\frac{2}{L}\right]^{\frac{3}{2}} \text{ and } \Psi(\vec{r},t) = \left[\frac{2}{L}\right]^{\frac{3}{2}} [\sin k_1 x \sin k_2 y \sin k_3 z] e^{i\frac{E}{\hbar}t}$$





















Deconstructing The Schrodinger Equation for Hydrogen Now go break up LHS to seperate the r & θ terms..... LHS: $\frac{\sin^2 \theta}{R} \frac{\partial}{\partial r} \left(r^2 \frac{\partial R}{\partial r} \right) + \frac{\sin \theta}{\Theta} \frac{\partial}{\partial \theta} \left(\sin \theta \frac{\partial \Theta}{\partial \theta} \right) + \frac{2mr^2 \sin^2 \theta}{\hbar^2} (E + \frac{ke^2}{r}) = m_l^2$ Divide Thruout by $\sin^2 \theta$ and arrange all terms with r away from $\theta \Rightarrow$ $\frac{1}{R} \frac{\partial}{\partial r} \left(r^2 \frac{\partial R}{\partial r} \right) + \frac{2mr^2}{\hbar^2} (E + \frac{ke^2}{r}) = \frac{m_l^2}{\sin^2 \theta} - \frac{1}{\Theta} \frac{\partial}{\partial \theta} \left(\sin \theta \frac{\partial \Theta}{\partial \theta} \right)$ Same argument : LHS is fn of r, RHS is fn of θ ; For them to be equal for all $r, \theta \Rightarrow$ LHS = const = RHS = l(l+1)What is the mysterious l(l+1)? Just a number like 2(2+1)

So What do we have after all the shuffling!

$$\frac{d^{2}\Phi}{d\phi^{2}} + m_{l}^{2}\Phi = 0.....(1)$$

$$\frac{1}{\sin\theta} \frac{d}{d\theta} \left(\sin\theta \frac{d\Theta}{d\theta}\right) + \left[l(l+1) - \frac{m_{l}^{2}}{\sin^{2}\theta}\right] \Theta(\theta) = 0....(2)$$

$$\frac{1}{r^{2}} \frac{d}{dr} \left(r^{2} \frac{\partial R}{\partial r}\right) + \left[\frac{2mr^{2}}{\hbar^{2}} (E + \frac{ke^{2}}{r}) - \frac{l(l+1)}{r^{2}}\right] R(r) = 0....(3)$$
These 3 "simple" diff. eqn describe the physics of the Hydrogen atom.
All we need to do now is guess the solutions of the diff. equations
Each of them, clearly, has a different functional form







The Hydrogen Wavefunction: $\psi(r, \theta, \phi)$ and $\Psi(r, \theta, \phi, t)$ To Summarize : The hydrogen atom is brought to you by the letters: $\begin{bmatrix}n = 1, 2, 3, 4, 5, \dots, \infty \\ l = 0, 1, 2, 3, 4, \dots, (n-1) \\ m_l = 0, \pm 1, \pm 2, \pm 3, \dots, \pm l \end{bmatrix}$ Quantum # appear only in Trapped systems $\psi(r, \theta, \phi) = R_{nl}(r) \cdot \Theta_{lm_l}(\theta) \quad \Phi_{m_l}(\phi) = R_{nl}Y_l^{m_l}$ The Spatial part of the Hydrogen Atom Wave Function is: $\psi(r, \theta, \phi) = R_{nl}(r) \cdot \Theta_{lm_l}(\theta) \quad \Phi_{m_l}(\phi) = R_{nl}Y_l^{m_l}$ $Y_l^{m_l} \text{ are known as Spherical Harmonics. They define the angular structure in the Hydrogen-like atoms.$ The Full wavefunction is $\Psi(r, \theta, \phi, t) = \psi(r, \theta, \phi)e^{-\frac{iE}{h}t}$



$l \rightarrow s (l=0) p (l=1) d (l)$ n \downarrow $1 1s$ $2 2s 2p$ $3 3s 3p 3d$ $4 4s 4p 4d$ $5 5s 5p 5d$ Note that: $\bullet n = 1 \text{ is a non-degenerate system}$ $\bullet n > 1 \text{ are all degenerate in } l \text{ and } m$ All states have same energy But different angular configure	iic States in Hydrogen
n \downarrow 1 1s 2 2s 2p 3 3s 3p 3d 4 4s 4p 4d 5 5s 5p 5d Note that: •n =1 is a non-degenerate system •n>1 are all degenerate in <i>l</i> and <i>m</i> All states have same energy But different angular configurence	2) $f(l=3)$ $g(l=4)$
↓ 1 1s 2 2s 2p 3 3s 3p 3d 4 4s 4p 4d 5 5s 5p 5d ote that: •n =1 is a non-degenerate system •n>1 are all degenerate in <i>l</i> and <i>m</i> All states have same energy But different angular configure	
11s22s2p33s3p44s4p55s5p5dote that:•n =1 is a non-degenerate system•n>1 are all degenerate in l and m All states have same energy Put different angular configure	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	
3 $3s$ $3p$ $3d$ 4 $4s$ $4p$ $4d$ 5 $5s$ $5p$ $5d$ ote that:•n =1 is a non-degenerate system•n>1 are all degenerate in l and m All states have same energyPut different angular configure	
44s4p4d55s5p5dote that:•n =1 is a non-degenerate system•n>1 are all degenerate in l and mAll states have same energyPut different angular configure	
5 5s 5p 5d ote that: •n =1 is a non-degenerate system •n>1 are all degenerate in l and m All states have same energy Put different angular configure	4f
 •n =1 is a non-degenerate system •n>1 are all degenerate in <i>l</i> and <i>m</i>. All states have same energy Put different angular configure 	5 <i>f</i> 5 <i>g</i>
 n =1 is a non-degenerate system n>1 are all degenerate in <i>l</i> and <i>m</i>. All states have same energy Put different angular configure 	
•n>1 are all degenerate in <i>l</i> and <i>m</i> All states have same energy But different engular configur	$ke^{2}(1)$
All states have same energy	$E=-\frac{KC}{-1}$
Dut different engular configu	$2a_0 \setminus n^2$
But unrerent angular configu	tion







Interpreting Orbital Quantum Number (l)
Radial part of S.Eqn: $\frac{1}{r^2} \frac{d}{dr} \left(r^2 \frac{dR}{dr} \right) + \left[\frac{2m}{\hbar^2} \left(E + \frac{ke^2}{r} \right) - \frac{l(l+1)}{r^2} \right] R(r) = 0$
For H Atom: $E = K + U = K_{RADIAL} + K_{ORBITAL} - \frac{ke^2}{r}$; substitute this in E
$\frac{1}{r^2}\frac{d}{dr}\left(r^2\frac{dR}{dr}\right) + \frac{2m}{\hbar^2}\left[K_{\text{RADIAL}} + K_{\text{ORBITAL}} - \frac{\hbar^2}{2m}\frac{l(l+1)}{r^2}\right]R(r) = 0$
Examine the equation, if we set $K_{\text{ORBITAL}} = \frac{\hbar^2}{2m} \frac{l(l+1)}{r^2}$ then
what remains is a differential equation in r
$\frac{1}{r^2} \frac{d}{dr} \left(r^2 \frac{dR}{dr} \right) + \frac{2m}{\hbar^2} \left[K_{\text{RADIAL}} \right] R(r) = 0 \text{ which depends only on radius r of orbit}$
Further, we also know that $K_{ORBITAL} = \frac{1}{2}mv_{orbit}^2$; $\vec{L} = \vec{r} \times \vec{p}$; $ L = mv_{orb}r \Rightarrow K_{ORBITAL} = \frac{L^2}{2mr^2}$
Putting it all togather: $K_{\text{ORBITAL}} = \frac{\hbar^2}{2m} \frac{l(l+1)}{r^2} = \frac{L^2}{2mr^2} \Rightarrow \text{ magnitude of Ang. Mom} L = \sqrt{l(l+1)}\hbar$
Since $l = positive$ integer=0,1,2,3(n-1) \Rightarrow angular momentum $ L = \sqrt{l(l+1)}\hbar = discrete \ values$
$ L = \sqrt{l(l+1)}\hbar$: QUANTIZATION OF Electron's Angular Momentum














TABLE 7-1 Spherical harmonics							
l = 0	m = 0	$Y_{00} = \sqrt{\frac{1}{4\pi}}$					
<i>l</i> = 1	m = 1	$Y_{11} = -\sqrt{\frac{3}{8\pi}}\sin\theta \ e^{i\phi}$					
	m = 0	$Y_{10} = \sqrt{\frac{3}{4\pi}} \cos \theta$					
	m = -1	$Y_{1-1} = \sqrt{\frac{3}{8\pi}} \sin \theta \ e^{-i\phi}$					
<i>l</i> = 2	<i>m</i> = 2	$Y_{22} = \sqrt{\frac{15}{32\pi}} \sin^2 \theta \ e^{2i\phi}$					
	m = 1	$Y_{21} = -\sqrt{\frac{15}{8\pi}}\sin\theta\cos\theta e^{i\phi}$					
	m = 0	$Y_{20} = \sqrt{\frac{5}{16\pi}} (3\cos^2\theta - 1)$					
	m = -1	$Y_{2-1} = \sqrt{\frac{15}{8\pi}} \sin \theta \cos \theta \ e^{-i\phi}$					
	m = -2	$Y_{2-2} = \sqrt{\frac{15}{32\pi}} \sin^2 \theta \ e^{-2i\phi}$					





Designer Wave Functions: Solutions of S. Eq ! Linear Superposition Principle means allows me to "cook up" wavefunctions $\psi_{2p_x} = \frac{1}{\sqrt{2}} [\psi_{211} + \psi_{21-1}]$ has electron "cloud" oriented along x axis $\psi_{2p_y} = \frac{1}{\sqrt{2}} [\psi_{211} - \psi_{21-1}]$ has electron "cloud" oriented along y axis So from 4 solutions $\psi_{200}, \psi_{210}, \psi_{211}, \psi_{21-1} \rightarrow 2s, 2p_x, 2p_y, 2p_z$

Similarly for n=3 states ...and so on ...can get very complicated structure in $\theta \& \phi$which I can then mix & match to make electrons "most likely" to be where I want them to be !











In formulating the Hydrogen Atom, Bohr was obliged to postulate that the frequency of radiation emitted by an atom dropping from energy level E_m to a lower level E_n is: $\boxed{f = \frac{E_m - E_n}{h}}$ This relationship rises naturally in Quantum Mechanics, consider for simplicity a system in which an electron only in the x direction: The time-dependent Wavefunction $\Psi_n(x,t) = \psi_n(x)e^{\frac{iE_n}{h}t}$; $<x>=\int_{-\infty}^{\infty} x \ \psi_n^* \psi_n dx = \text{ constant in time, does not oscillate, no radiation occurs}$ But, due to an external perturbation lasting some time, electron shifts from one state (m) to another(n) In this period wavefunction of electron is a linear superposition of two possible states $\Psi=a\Psi_n + b\Psi_m$; $a^*a = \text{ prob. of electron in state n and b^*b = \text{ prob. of electron in state m; } [a^*a+b^*b=1]$ Initially a=1,b=0 and finally a=0,b=1. While the electron is in either state there is no radiation but when it is in the midst of transition from $m \to n$, both a and b have non-vanishing values and radiation is produced. Expectation value for compositive wavefunction $<x> = \int x\Psi^*\Psi dx$; $<x>=\int_{-\infty}^{\infty} x(a^2\Psi_n^*\Psi_n + b^*a\Psi_m^*\Psi_n + a^*b\Psi_n^*\Psi_m + b^2\Psi_m^*\Psi_m)dx$

Transition Between States In Quantum Systems $<x>= \int_{-\infty}^{\infty} x(a^{2}\Psi_{n}^{*}\Psi_{n} + b^{*}a\Psi_{m}^{*}\Psi_{n} + a^{*}b\Psi_{n}^{*}\Psi_{m} + b^{2}\Psi_{m}^{*}\Psi_{m})dx$ $<x>= a^{2}\int x\Psi_{n}^{*}\Psi_{n}dx + b^{2}\int x\Psi_{m}^{*}\Psi_{m}dx$ $+ ab^{*}\int x\Psi_{m}^{*}e^{+i(E_{m}/\hbar)t}\Psi_{n}e^{-i(E_{n}/\hbar)t}dx + a^{*}b\int x\Psi_{n}^{*}e^{+i(E_{n}/\hbar)t}\Psi_{m}e^{-i(E_{m}/\hbar)t}dx$

Use $e^{i\theta} = \cos\theta + i\sin\theta$ and $e^{-i\theta} = \cos\theta - i\sin\theta$ in the above and consider just the REAL part of expression for the last two terms, it varies with time as

$$\cos\left(\frac{\mathbf{E}_{\mathrm{m}} - \mathbf{E}_{\mathrm{n}}}{\hbar}\right) t = \cos 2\pi \left(\frac{\mathbf{E}_{\mathrm{m}} - \mathbf{E}_{\mathrm{n}}}{h}\right) t = \cos 2\pi \mathrm{ft}$$

So the $\langle x \rangle$ of the electron oscillates with frequency f and one has a nice electric dipole analogy \Rightarrow Hence radiative transitons ! Similarly for particle in an infinite well or harmonic oscillator ...

300























































Topics In Particle Physics
Cosmic Messengers!
Dirac, Anderson and the Positron !• antimatter
 Fundamental forces in nature
How elementary particles are produced: Accelerators
 Classification of Particle and How we know this – Conservation laws
 Colored Quarks and Quantum Chromodynamics!
Electroweak theory and Standard model
The Higgs Particle and Large Hadron Collider
Beyond the Standard model : Supersymmetry & Strings







Powe	er of I	Microscope		_
	\$			
Wavelen smaller	gth of pro than the	bbe radiation should b object to be resolved	e	
	$\lambda \ll \frac{1}{2}$	$\frac{h}{p} = \frac{hc}{E}$		
Object	Size	Energy of Radiation		
Atom	10-10 m	0.00001 GeV (electrons)		
Nucleon	10-15m	0.01 GeV (alphas)		
Quarks	?	> 1 GeV (electrons)		
Radioactive Need	sources giv	e energies in the range of Me ors for higher energies.	eV	
		"electronic eyes"		







- Anderson's discovery of positron !



















Table 15.1 Par	rticle Interacti	one			
Interaction (Force)	Particles Acted on by Force	Relative Strength"	Typical Lifetimes for Decays via a Given Interaction	Range of Force	Force- Carrying Particle Exchanged
Strong	Quarks,	1	$\leq 10^{-20}$ s	Short (≈1 fm)	Gluon
Electromagnetic	Charged	$\approx 10^{-2}$	$\approx 10^{-16}$ s	Long (∞)	Photon
Wcak	Quarks,	$\approx 10^{-6}$	$\geq 10^{-10} s$	Short ($\approx 10^{-3}$ fm)	W^{\pm} , Z^0 bosons
Gravitational	All particles	$\approx 10^{-43}$	5	Long (∞)	Graviton ^b
^a For two <i>u</i> quarks at 5 ^b Not experimentally	3×10^{-17} m. detected.	1152 X -41	1-1.2	n succession	N













Category	Particle Name	Symbol	Anti- particle	Mass (MeV/c ²)	B	Le	L_{μ}	L_{τ}	s	Lifetime (s)	Principal Decay Modes ^a
Leptons	Electron	e ⁻	e ⁺	0.511	0	+1	0	0	0	Stable	
-	Electron-neutrino	ν_c	$\overline{\nu}_{c}$	$<2.8 \times 10^{-6}$	0	+1	0	0	0	Stable	
	Muon	μ-	μ*	105.7	0	0	+1	0	0	2.19×10^{-6}	$e^- \overline{\nu}_{\nu} \nu_{\nu}$
	Muon-neutrino	ν_{μ}	$\bar{\nu}_{\mu}$	$<3.5 \times 10^{-6}$	0	0	+1	0	0	Stable	e rerµ
	Tau	τ^{-}	τ^{\mp}	1784	0	0	0	+1	0	3.3×10^{-13}	$\mu^- \overline{\nu}_\mu \nu_\tau$, $e^- \overline{\nu}_\mu \nu_\tau$
	Tau-neutrino	ν_{τ}	$\overline{\nu}_{\tau}$	${<}8.4 imes10^{-6}$	0	0	0	$^{+1}$	0	Stable	e 1817
Hadrons											
Mesons	Pion	π^+	π^{-}	139.6	0	0	0	0	0	2.60×10^{-8}	$\mu^+ \nu_{}$
		π^0	Self	135.0	0	0	0	0	0	0.83×10^{-16}	27
	Kaon	K ⁺	K-	493.7	0	0	0	0	+1	1.24×10^{-8}	$\mu^{+}\nu_{\mu}$ $\pi^{+}\pi^{0}$
		K_S^0	\overline{K}_{S}^{0}	497.7	0	0	0	0	+1	0.89×10^{-10}	$\pi^{+}\pi^{-}$ $2\pi^{0}$
		K_L^0	\overline{K}_{L}^{0}	497.7	0	0	0	0	+1	$5.2 imes10^{-8}$	$\pi^{\pm}c^{\mp}\overline{\nu}_{c}$ $3\pi^{0}$
	Fra	_	6-16							-10-19	$\pi^-\mu^+\nu_\mu$
	Eta	η.	Self E-10	059	0	0	0	0	0	<10-10	$2\gamma, 3\pi^{0}$
_	_	η	Seif	908	0	0	0	0	0	2.2×10^{-11}	$\eta \pi^+ \pi^-$
Baryons	Proton	р	P	938.3	+1	0	0	0	0	Stable	
	Neutron	n	n	939.6	+1	0	0	0	0	624	$pe^- \overline{\nu}_c$
	Lambda	Λ^0	Λ^0	1115.6	+1	0	0	0	$^{-1}$	2.6×10^{-10}	$p\pi^{-}, n\pi^{0}$
	Sigma	Σ*	Σ^{-}	1189.4	+1	0	0	0	$^{-1}$	0.80×10^{-10}	$p\pi^0$, $n\pi^+$
		Σ^0	Σ ⁰	1192.5	+1	0	0	0	$^{-1}$	6×10^{-20}	$\Lambda^{0}\gamma$
		Σ.	Σ^+	1197.3	+1	0	0	0	-1	$1.5 imes 10^{-10}$	$n\pi^{-}$
	Delta	Δ^{++}	$\underline{\Delta}$	1230	+1	0	0	0	0	6×10^{-24}	$p\pi^+$
		Δ'	$\frac{\Delta}{10}$	1231	+1	0	0	0	0	6×10^{-24}	$p\pi^0$, $n\pi^+$
		Δ ^{.0}	$\frac{\Delta^3}{\Delta^4}$	1232	+1	0	0	0	0	6×10^{-24}	$n\pi^0$, $p\pi^-$
	¥!	Δ_ 	$\frac{\Delta^+}{\Xi_0}$	1234	+1	0	0	0	0	6×10^{-24}	$n\pi^{-}$
	л	H-	H+	1315	+1	0	0	0	-2	2.9×10^{-10}	$\Lambda^0 \pi^0$
	Omer		=+ 0+	1321	+1	0	0	0	-2	1.64×10^{-10}	$\Lambda^0 \pi^-$
	Omega	11	M_{+}	1672	+1	0	0	0	-3	0.82×10^{-10}	$\Xi^{-}\pi^{0}, \Xi^{0}\pi^{-},$
											$\Lambda^{0}K^{-}$






































sses of Fundamental Part	of Fundamental Particles		Bosons That Mediate the Basic Interactions							
Particle	Mass	Interaction	B	loson	Spin	Mass	Electric Charge			
Quarks		Strong	g	(gluon)†	1	0	0			
Quarks		Weak	V	V±	1	$80.22 \text{ GeV}/c^2$	$\pm 1e$			
<i>u</i> (up)	$336 \text{ MeV}/c^2$	1993	Z	0	1	91.19 GeV/c ²	0			
d (down)	$338 \text{ MeV}/c^2$	Electromagn	etic γ	(photon)	1	0	0			
s (strange)	540 MeV/ c^{2}	Gravitationa	1 0	iraviton [*]	2	0	0			
c (charmed)	1,500 MeV/c ²	† Not yet observed.								
<i>t</i> (top)	$174,000 \text{ MeV}/c^2$									
b (bottom)	$4{,}500~{\rm MeV}/c^2$					s	trong			
Leptons			Gravitational	Weak	Electromagnet	ic Fundamental	Residual			
e^- (electron)	$0.511 \text{ MeV}/c^2$	Acts on Particlas avpariancing	Mass	Flavor Outsike Jantone	Electric charge Electrically cha	Color charge	Hadrone			
v. (electron neutrino)	$< 7 {\rm eV}/c^2$	Particles mediating	Graviton	W [±] , Z	γ	Gluons	Mesons			
e (muon)	105 659 MoV/c2	Strength for two quarks at 10 ⁻¹⁸ m ⁴	10-41	0.8	1	25	(not applicab			
μ (muon)	105.659 Ivie v / C ²	Strength for two protons in nucleus ¹	10-36	10-7	1	(not applicable)	20			
v_{μ} (muon neutrino)	$< 0.27 \text{ MeV}/c^2$	engths are relative to electromag	netic strength.							
$ au^-$ (tau)	$1,784 \text{ MeV}/c^2$									

Flavor	Spin	Charge	Baryon	Strangeneon	Charm	Tonnoon	Battompoor	
FIAVUI	Spin	Charge	Number	Strangeness	Griariti	iopriess	Douorniess	
Quarks								
и (up)	$\frac{1}{2}\hbar$	$+\frac{2}{3}e$	$+\frac{1}{3}$	0	0	0	0	
d (down)	$\frac{1}{2}\hbar$	$-\frac{1}{3}e$	$+\frac{1}{3}$	0	0	0	0	
s (strange)	$\frac{1}{2}\hbar$	$-\frac{1}{3}e$	$+\frac{1}{3}$	-1	0	0	0	
c (charmed)	$\frac{1}{2}\hbar$	$+\frac{2}{3}e$	$+\frac{1}{3}$	0	+1	0	0	
t (top)	$\frac{1}{2}\hbar$	$+\frac{2}{3}e$	$+\frac{1}{3}$	0	0	+1	0	
b (bottom)	$\frac{1}{2}\hbar$	$-\frac{1}{3}e$	$+\frac{1}{3}$	0	0	0	+1	
Antiquarks								
ū	$\frac{1}{2}\hbar$	$-\frac{2}{3}e$	$-\frac{1}{3}$	0	0	0	0	
d	$\frac{1}{2}\hbar$	$+\frac{1}{3}e$	$-\frac{1}{3}$	0	0	0	0	
\overline{s}	$\frac{1}{2}\hbar$	$+\frac{1}{3}e$	$-\frac{1}{3}$	+1	0	0	0	
ī	$\frac{1}{2}\hbar$	$-\frac{2}{3}e$	$-\frac{1}{3}$	0	-1	0	0	
ī	$\frac{1}{2}\hbar$	$-\frac{2}{3}e$	$-\frac{1}{3}$	0	0	-1	0	
\overline{b}	$\frac{1}{2}\hbar$	$+\frac{1}{3}e$	-1	0	0	0	-1	







