

































Relativistic Work Done & Change in Energy

$$W = \int_{x_1}^{x_2} \vec{F} \cdot d\vec{x} = \int_{x_1}^{x_2} \frac{d\vec{p}}{dt} \cdot d\vec{x}$$

$$p = \frac{mu}{\sqrt{1 - \frac{u^2}{c^2}}} \quad \therefore \quad \frac{d\vec{p}}{dt} = \frac{m\frac{du}{dt}}{\left[1 - \frac{u^2}{c^2}\right]^{3/2}},$$
substitute in W,

$$\therefore \quad W = \int_{0}^{u} \frac{m\frac{du}{dt}udt}{\left[1 - \frac{u^2}{c^2}\right]^{3/2}} \quad \text{(change in var } \mathbf{x} \to \mathbf{u}\text{)}$$











Relativistic Kinetic Energy & Newtonian Physics	
Relativistic KE $K = \gamma mc^2 - mc^2$	
$\begin{bmatrix} \text{Remember Binomial Theorem} \\ \text{for } x \ll 1; \ (1+x)^n = (1+\frac{nx}{1!}+\frac{n(n-1)}{2!}x^2 + \text{smaller terms}) \end{bmatrix}$ $\therefore \text{ When } u \ll c, \ \left[1-\frac{u^2}{c^2}\right]^{-\frac{1}{2}} \cong 1+\frac{1}{2}\frac{u^2}{c^2} + \dots \text{ smaller terms} \\ \text{so } K \cong mc^2[1+\frac{1}{2}\frac{u^2}{c^2}] - mc^2 = \frac{1}{2}mu^2 \text{ (classical form recovered)} \end{bmatrix}$	
Total Energy of a Particle $E = \gamma mc^2 = KE + mc^2$	
For a particle at rest, $u = 0 \implies \text{Total Energy } \text{E}=\text{mc}^2$	





Lowering Fuel Core in a Nuclear Reactor

First Nuke Reactor : Pennsylvania 1957

Pressure Vessel contains : 14 Tons of Natural Uranium + 165 lb of enriched Uranium

Power plant rated at 90MW, Retired (82)

Pressure vessel packed with Concrete now sits in Nuclear Waste Facility in Hanford, Washington

Nuclear Fusion : What Powers the Sun

Opposite of Fission

Mass of a Nucleus < mass of its component protons+Neutrons Nuclei are stable, bound by an attractive "Strong Force" Think of Nuclei as molecules and proton/neutron as atoms making it Binding Energy: Work/Energy required to pull a bound system (M) apart leaving its components (m) free of the attractive force and at rest:

> $Mc^2 + BE = \sum_{i=1}^{n} m_i c^2$ ${}^{2}_{1}H = {}^{4}_{2}He + 23.9 \text{ MeV} =$ **Deuterium =** Helium + Released Energy

Deuterium

 $^{2}_{1}\mathrm{H}$

Think of energy released in Fusion as Dissociation energy of Chemistry

Sun's Power Output = 4×10^{26} Watts $\Rightarrow 10^{38}$ Fusion/Second !!!!

