



Department of Physics
University of California San Diego

Modern Physics (2D)
Prof. V. Sharma
Quiz #1 (Jan 17 2003)

Some Relevant Formulae, Constants and Identities

Speed of Light, $c = 3.0 \times 10^8 \text{ m/s}$

$$\gamma = \frac{1}{\sqrt{1 - v^2/c^2}}$$

$$x' = \gamma(x - vt)$$

$$t' = \gamma\left(t - \frac{vx}{c^2}\right)$$

$$u' = \frac{u - v}{1 - \frac{uv}{c^2}}$$

$$p = \frac{mu}{\sqrt{1 - u^2/c^2}}$$

$$E = \frac{mc^2}{\sqrt{1 - u^2/c^2}} = K + mc^2$$

$$f_{\text{obs}} = \frac{\sqrt{1 + v/c}}{\sqrt{1 - v/c}} f_{\text{source}}$$

Pl. write you answer in a Blue book in indelible ink. Make sure your code number is prominently displayed on each page



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Problem 1: Doppler Radar [8 pts]

If a police radar transmitter radiates at 10.0GHz, calculate the frequency shift observed by the police for a car traveling away from the police car at (a) 115 km/hr and (b) 130 km/hr (c) what measurement precision in frequency is required to distinguish between the two cars? State your answer as a fraction $\frac{\Delta f}{f}$.

Problem 2: Space talk [12 pts]

A observer on the Earth sees a rocket go by at a speed of $v=0.6c$.

(a) An astronaut on the rocket sends an escape pod back towards the Earth. She measures the speed of the escape pod to be $u=0.9c$.

What is the speed of the escape pod as measured by an observer on the Earth? (b) An observer on the escape pod measures the rocket to be 100 m long. What is the proper length of the rocket? (c) What is the length of the rocket as measured by an observer on Earth ?

Physics 2D: Quiz 1 Solutions

1] There are 2 Doppler shifts here: The one observed by the car, and the one the cop sees for the beam reflected from the car.

$$\text{First, } f_{\text{car}} = \sqrt{\frac{1-(v/c)}{1+(v/c)}} f_{\text{cop, original}}$$

This has the minus sign on the top b/c the relative motion is away from each other.

$$\text{Now, } f_{\text{cop, final}} = \sqrt{\frac{1-(v/c)}{1+(v/c)}} f_{\text{car}}$$

↑
What the cop measures.

$$\text{Thus } f_{\text{cop, final}} = \left[\frac{1 - \frac{v}{c}}{1 + \frac{v}{c}} \right] f_{\text{cop, original}}$$

$$a] v = 115 \frac{\text{km}}{\text{hr}} = \frac{115 \text{ km}}{1 \text{ hr}} \left(\frac{1 \text{ hr}}{3600 \text{ s}} \right) \left(\frac{10^3 \text{ m}}{1 \text{ km}} \right) = 31.9 \frac{\text{m}}{\text{s}}$$

So the freq. shift is

$$f_{\text{cop, final}} - f_{\text{cop, original}} = -2130 \text{ Hz}$$

Note that you can get this either by just plugging in
 or using the Taylor series $\frac{1-\frac{v}{c}}{1+\frac{v}{c}} \approx 1 - \frac{2v}{c}$, which

implies $f_{\text{cop, final}} - f_{\text{cop, orig}} = -\frac{2v}{c} f_{\text{cop, orig}}$. Same answer.

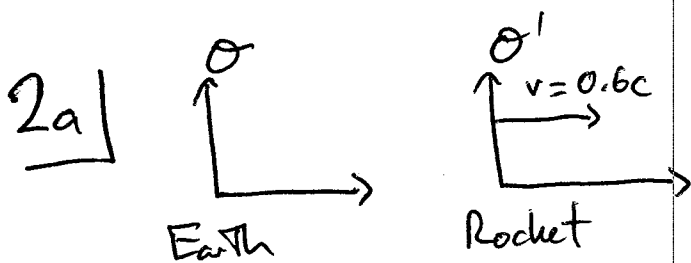
b) Now $v = 130 \frac{\text{km}}{\text{hr}} = 36.1 \frac{\text{m}}{\text{s}}$

So $f_{\text{cop, final}} - f_{\text{cop, original}} = -2407 \text{ Hz}$

c) The difference between these shifts is

$\Delta F = 2407 - 2130 \text{ Hz} = 277 \text{ Hz}$.

So $\frac{\Delta F}{f} = \frac{277 \text{ Hz}}{10^{10} \text{ Hz}} = 2.77 \times 10^{-8} \approx 3 \text{ parts in } 10^8$



The observer in O' measures $u' = -0.9c$.

So using $u = \frac{u' + v}{1 + \frac{u'v}{c^2}}$, we see $u = \frac{(-0.9 + 0.6)c}{1 + (-0.9)(0.6)}$

$= -0.65c$

So the speed (the mag. of the velocity) is $\boxed{0.65c}$.

b) The observer in the escape pod moves with speed $0.9c$ with respect to the rocket, so

$$L_{\text{pod}} = \sqrt{1 - (0.9)^2} L_{\text{rocket}}$$

$$(v/c, \frac{v^2}{c^2} = (0.9)^2)$$

↑
Length of rocket
measured in pod
frame

↑
Proper length
of rocket.

So using $L_{\text{pod}} = 100 \text{ m}$, we see

$$\boxed{L_{\text{rocket}} = 229 \text{ m}}$$

c) The observer on the Earth sees the rocket go by at $0.6c$.

$$\text{So } L_{\text{earth}} = \sqrt{1 - (0.6)^2} L_{\text{rocket}}$$

$$\boxed{L_{\text{earth}} = 184 \text{ m}}$$